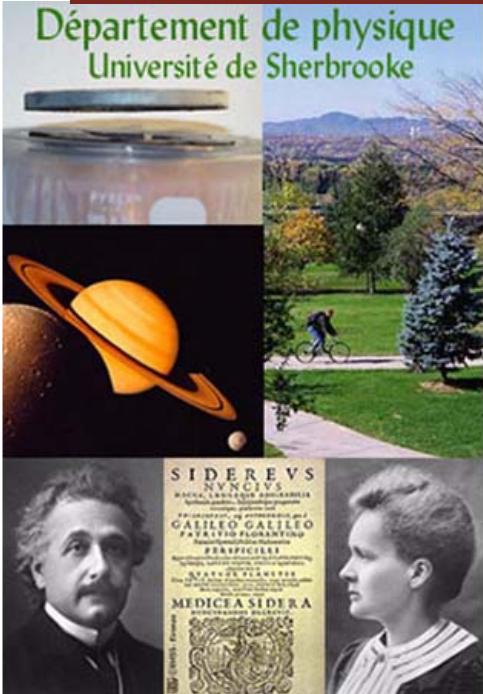
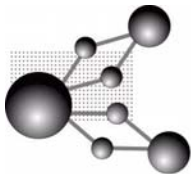


What is the Hamiltonian for parent high-temperature superconductors



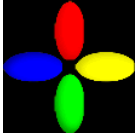
André-Marie Tremblay, Alexis Gagné-Lebrun



CENTRE DE RECHERCHE SUR LES PROPRIÉTÉS ÉLECTRONIQUES DE MATÉRIAUX AVANCÉS



Commanditaires:



Outline

- What is the problem?
- What is the numerical method?
- What are the results?
- Conclusion

What is the problem ?

Materials and theoretical considerations

Experiments

Previous theoretical work

What is the problem?

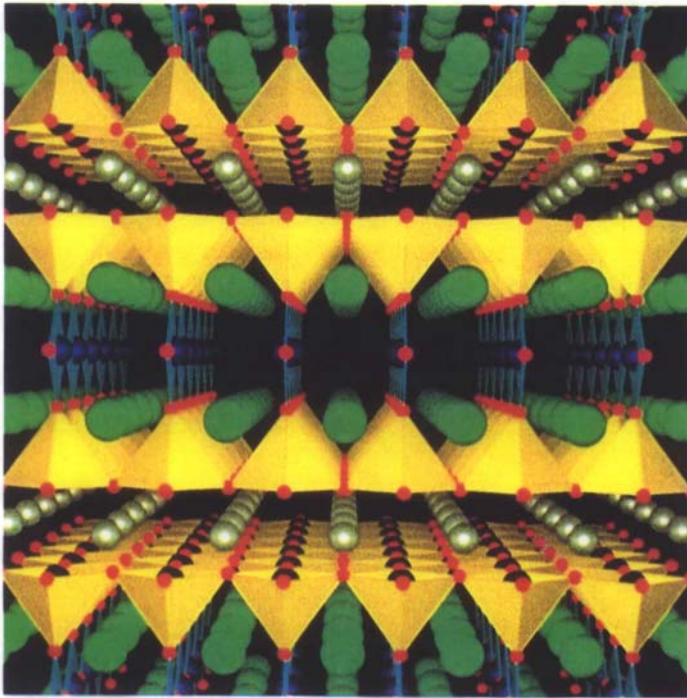
SCIENTIFIC AMERICAN

JUNE 1988
\$3.50

How nonsense is deleted from genetic messages.

Rx for economic growth: aggressive use of new technology.

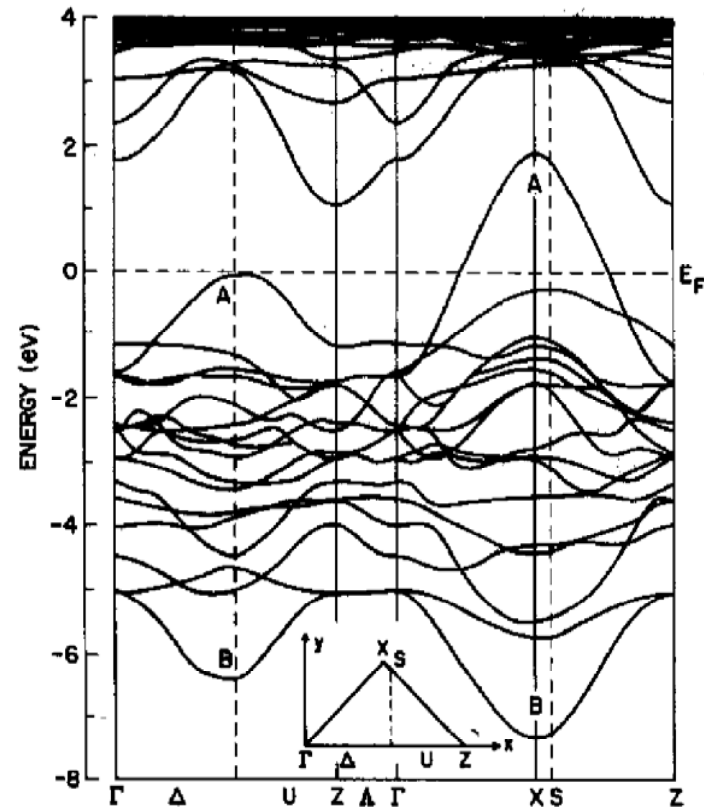
Can particle physics test cosmology?

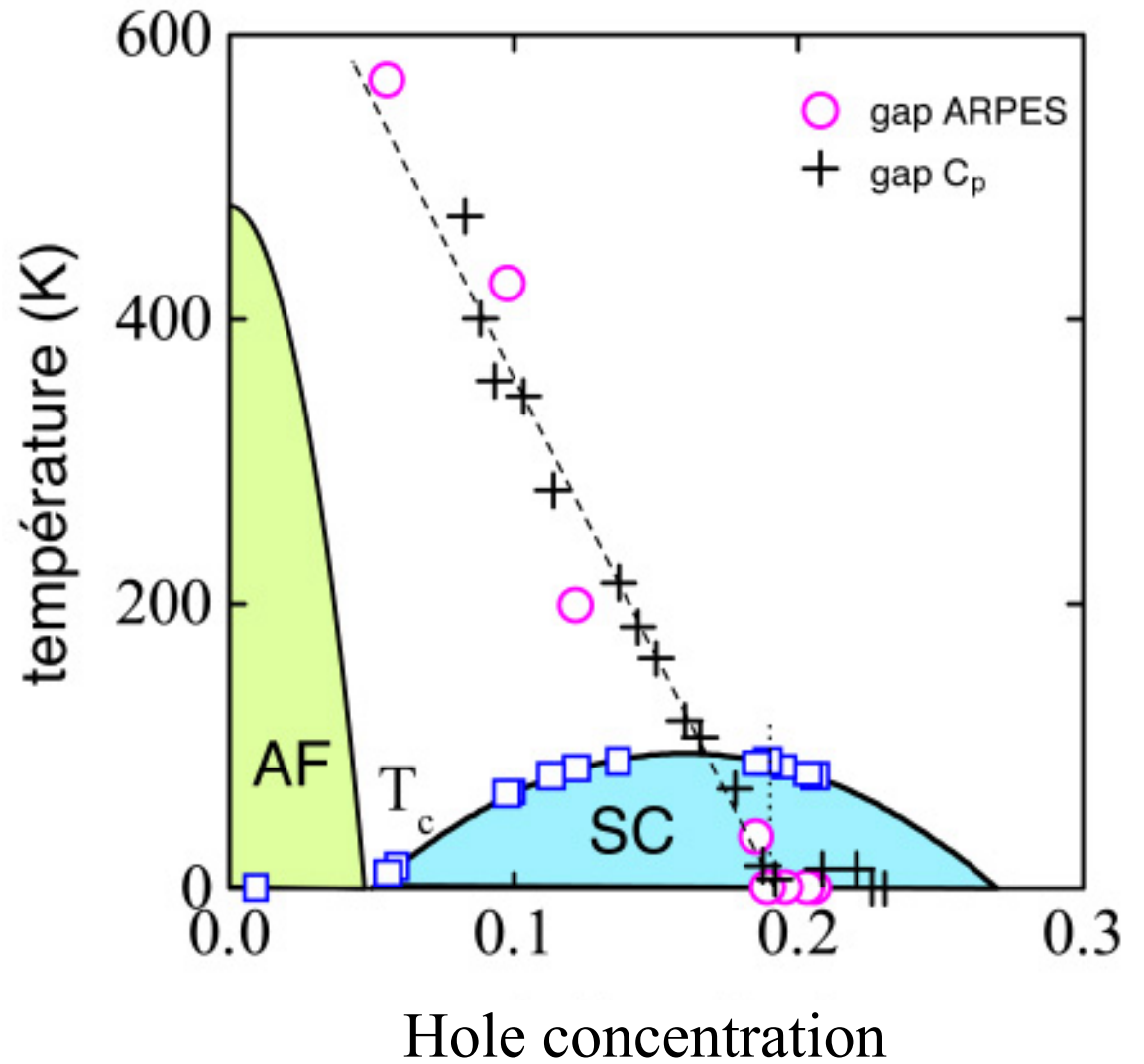
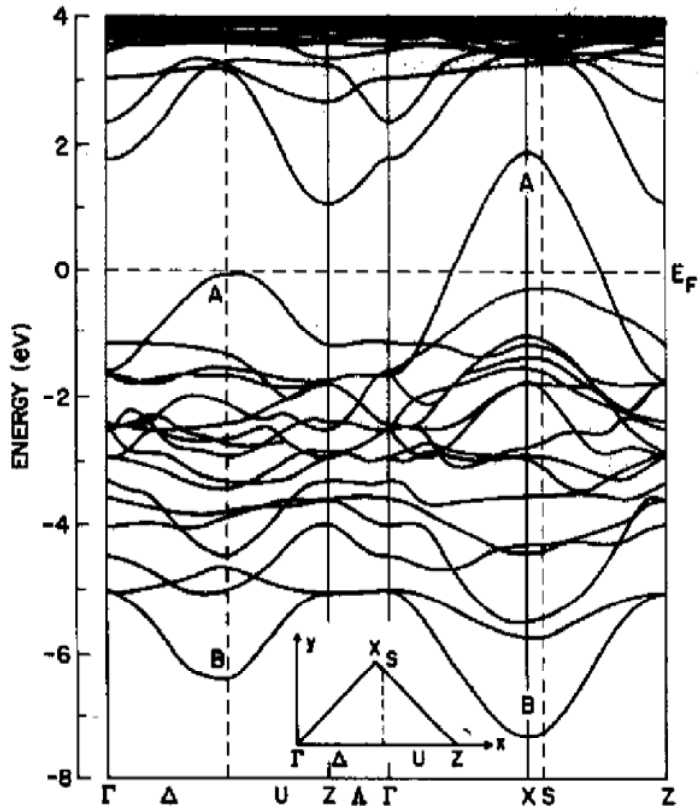


High-Temperature Superconductor belongs to a family of materials that exhibit exotic electronic properties.

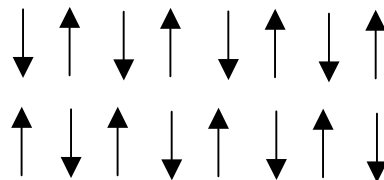


92-37





Antiferromagnet

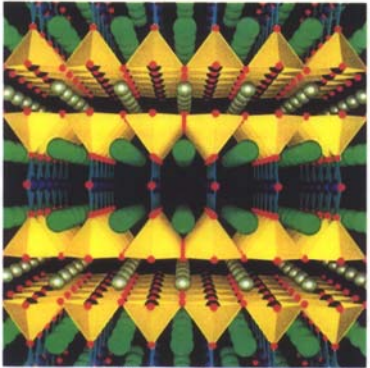


Residual interactions must be added to band structure

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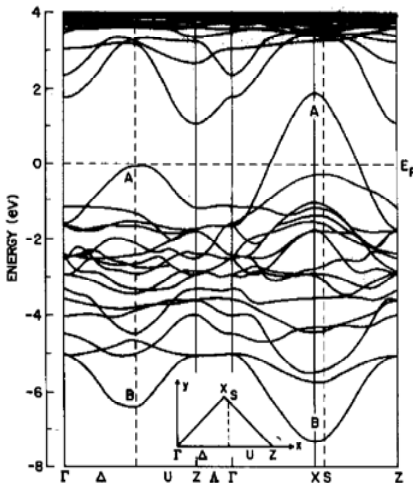
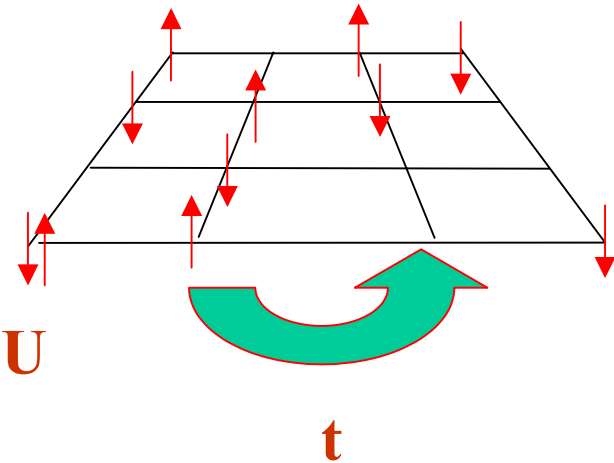
How nonsense is deleted from genetic messages.
 & for economic growth: aggressive use of new technology.
 Can particle physics test cosmology?



High-Temperature Superconductor belongs to a family of materials that exhibit exotic electronic properties.
 $\gamma\text{Ba}_2\text{Cu}_3\text{O}_{7-x}$ 93-37

The simplest model for Cu O_2 planes.

μ

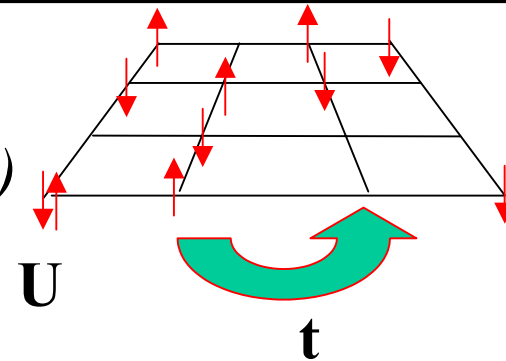


- Size of Hilbert space : 4^N (N = 16)
- With N=16, need 4 GigaBits just for states

Hubbard model (Kanamori, Gutzwiller, 1963) :

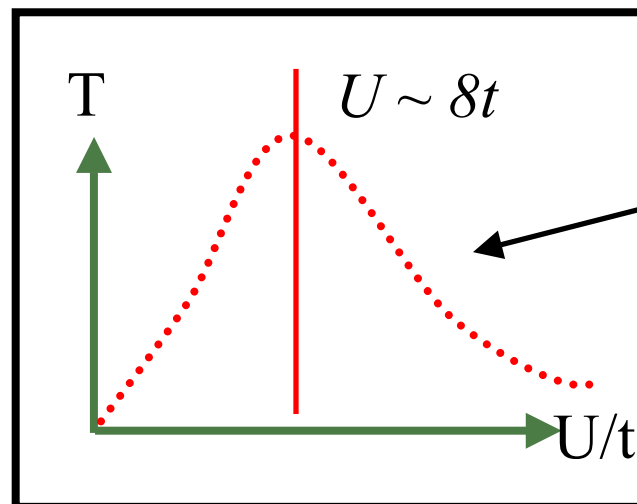
$$H = - \sum_{\langle ij \rangle \sigma} t_{ij} (c_{i\sigma}^\dagger c_{j\sigma} + c_{j\sigma}^\dagger c_{i\sigma}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

- « Screened » interaction U
- U, T smallest, $n = 1$ (ou $\delta = 1 - n$)
- $a = 1, t = 1, \hbar = 1$

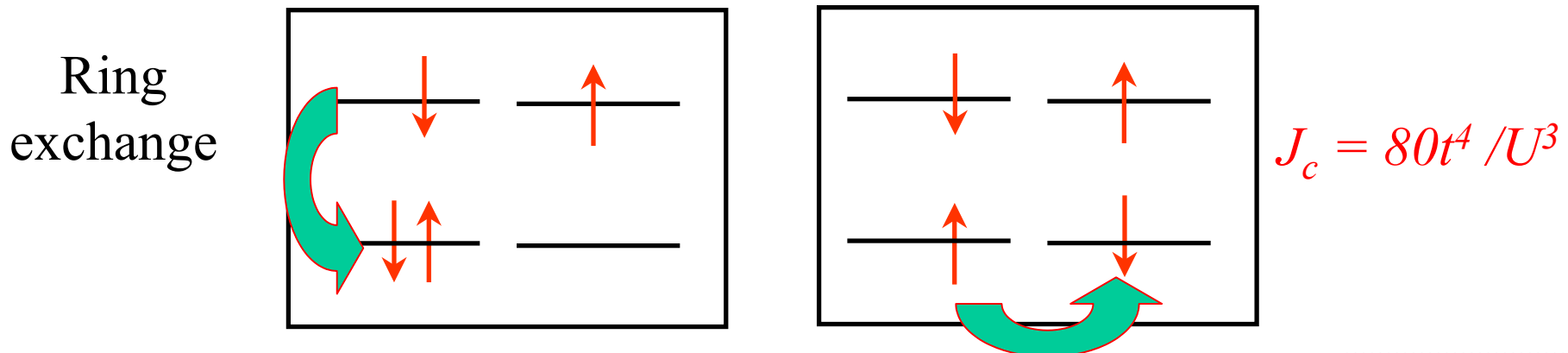
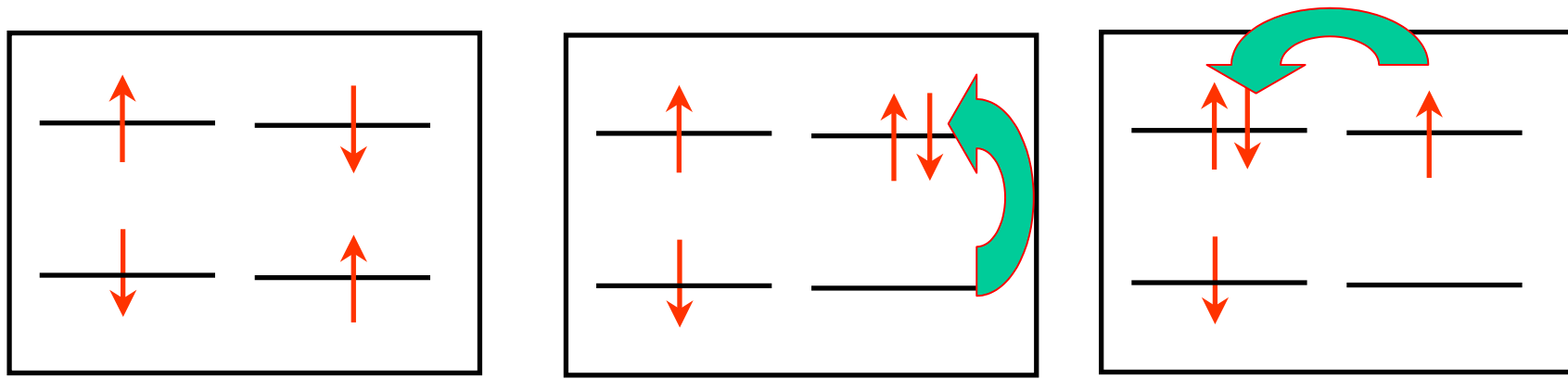
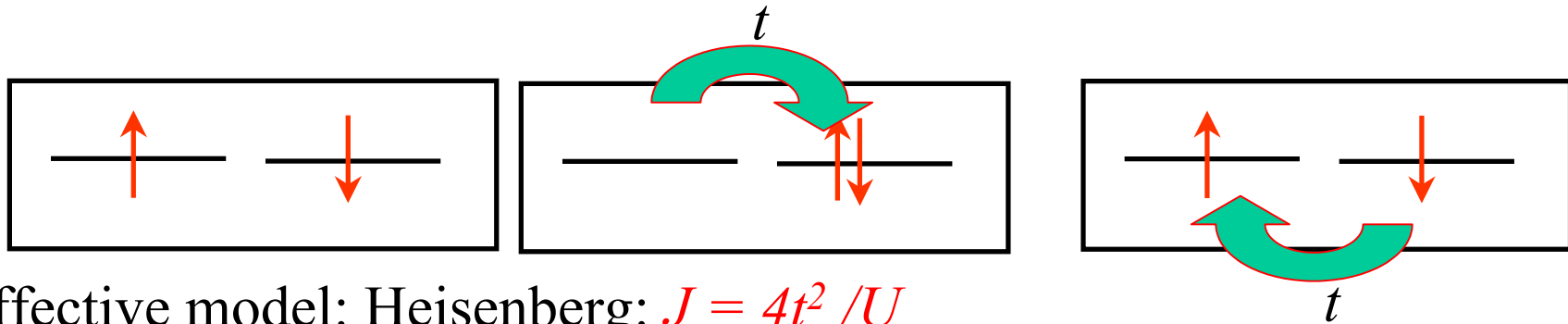


Strong vs weak coupling

- t from band structure,
- U harder



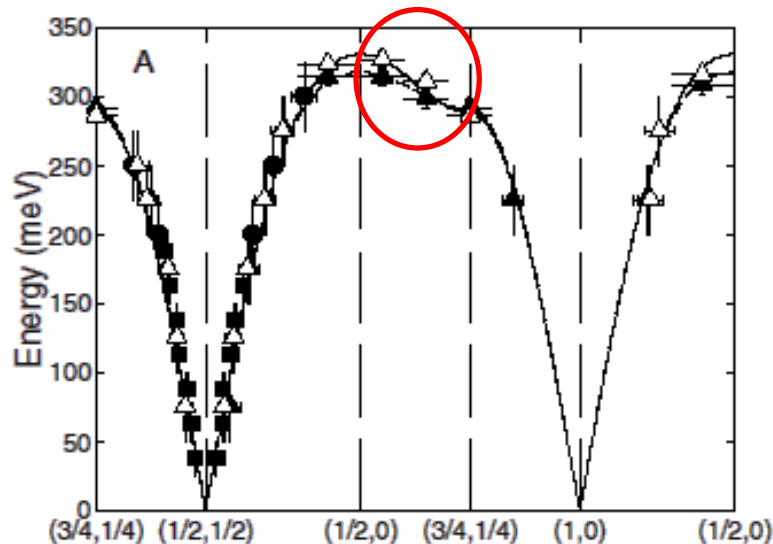
Strong
coupling



and second-neighbor hopping

Experimental approach and analysis

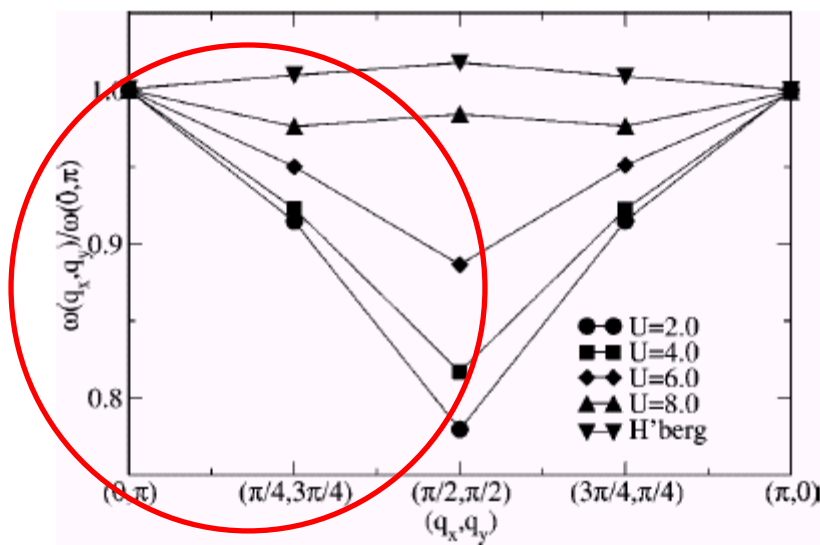
Experimental spin-wave dispersion



R. Coldea PRL **86**, 5377 (2001)

- Fitting the dispersion, knowing $J = 4t^2 / U$ and $J_c = 80t^4 / U^3$ determines both t and U .
- Find $U = 7.3 t$.
 - Beyond limit of validity of expansion in t/U
 - Use linear spin-wave analysis.

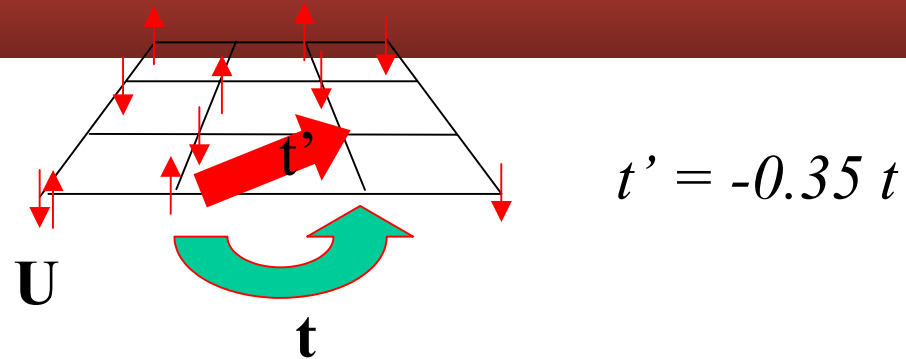
Some earlier theoretical work



P. Sengupta *et al.* Phys. Rev. B **66**, 144420 (2002)

- Quantum Monte Carlo simulations include quantum corrections (beyond linear spin waves)
- Limitation, SMA
- Find $U = 6t$
 - In agreement with RPA
 - Too small to fit optical gap at half-filling
 - Band structure effects should become more important

What we do here



- Quantum Monte Carlo with SMA for

$$H = -t \sum_{\langle \mathbf{i}, \mathbf{j} \rangle, \sigma} (c_{\mathbf{i}, \sigma}^\dagger c_{\mathbf{j}, \sigma} + c_{\mathbf{j}, \sigma}^\dagger c_{\mathbf{i}, \sigma})$$

$$- t' \sum_{\langle\langle \mathbf{i}, \mathbf{j} \rangle\rangle, \sigma} (c_{\mathbf{i}, \sigma}^\dagger c_{\mathbf{j}, \sigma} + c_{\mathbf{j}, \sigma}^\dagger c_{\mathbf{i}, \sigma}) + U \sum_{\mathbf{i}} n_{\mathbf{i}, \uparrow} n_{\mathbf{i}, \downarrow}$$

- Second-neighbor hopping, $t' = -0.35 t$

What is the method?

Quantum Monte Carlo calculations, including t'
Single Mode Approximation

$$\omega(\mathbf{q}) = 2S(\mathbf{q})/\chi(\mathbf{q})$$

How QMC works

Compute statistical averages with $\text{Tr}[e^{-\beta(H-\mu N)}]$

$$k_B = 1, t = 1, \beta = 1/T$$

Problem for importance sampling

$$H = K + V$$

$$[K, V] \neq 0$$

Trotter decomposition

$$e^{-\beta(H-\mu N)} = e^{-\Delta\tau(H-\mu N)} e^{-\Delta\tau(H-\mu N)} \dots e^{-\Delta\tau(H-\mu N)}$$

$$e^{-\Delta\tau(H-\mu N)} = e^{-\Delta\tau K} e^{-\Delta\tau(V-\mu N)} + O(\Delta\tau^2)$$

QMC, continued

Hubbard-Stratonovich transformation :

$$e^{-\Delta\tau U \left(n_{\mathbf{i},\uparrow} - \frac{1}{2}\right) \left(n_{\mathbf{i},\downarrow} - \frac{1}{2}\right)} = e^{-\Delta\tau U/4} \frac{1}{2} \sum_{x_i = \pm 1} e^{\lambda x_i (n_{\mathbf{i},\uparrow} - n_{\mathbf{i},\downarrow})}$$

$$\cosh(\lambda) = e^{\Delta\tau U/2}$$

Quantum Mechanical trace can be performed : gives a determinant

Determinant as a Boltzmann weight gives « sign problem ».

Put sign in observables.

Parameters for QMC calculations

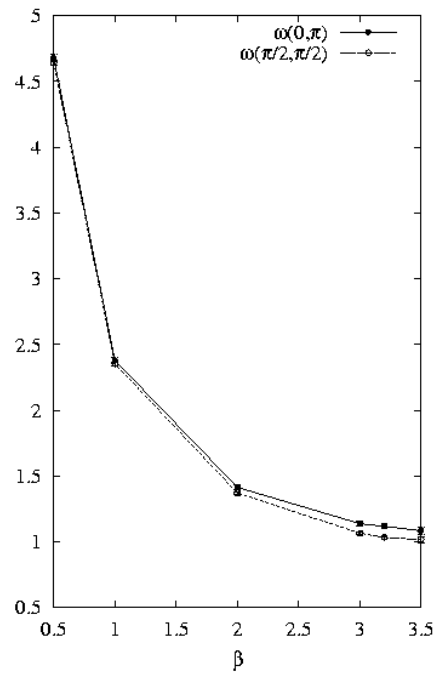
- Imaginary time discretization :
 $\Delta\tau = 1/10$ but same results as $\Delta\tau = 1/8$
- Gram-Schmidt every 5 time slices
- Estimator,
 $\langle S_z S_z \rangle$
- Measurements,
 1.25×10^5
- Block size for statistical error estimation, *250*

Technical details

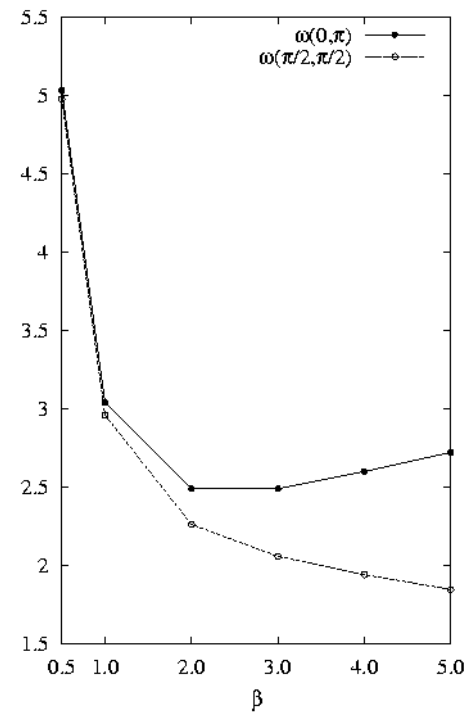
- Fortran 90
- ifc
- Scaling of computation time $L^6 N_\tau$
- One job for 12×12 with 10^5 measurements, 10^4 warmups takes 33 MB and 20 days on one CPU of elix 2 (*P IV*, 2.5 GHz)
- If distribute job on 10 nodes for 8×8 lattice, one run at fixed parameters takes one day on elix 1 (*P III*, 667 MHz).

Single-mode approximation

$$\omega(\mathbf{q}) = 2S(\mathbf{q})/\chi(\mathbf{q})$$



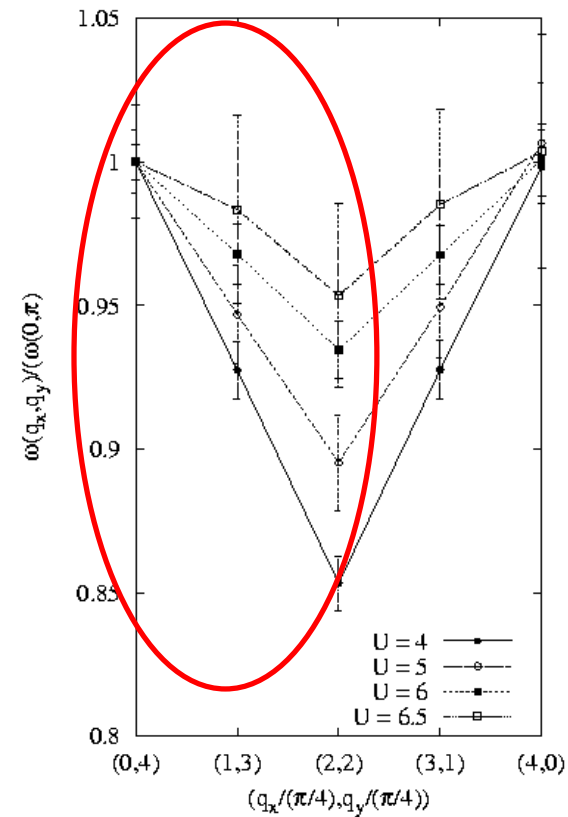
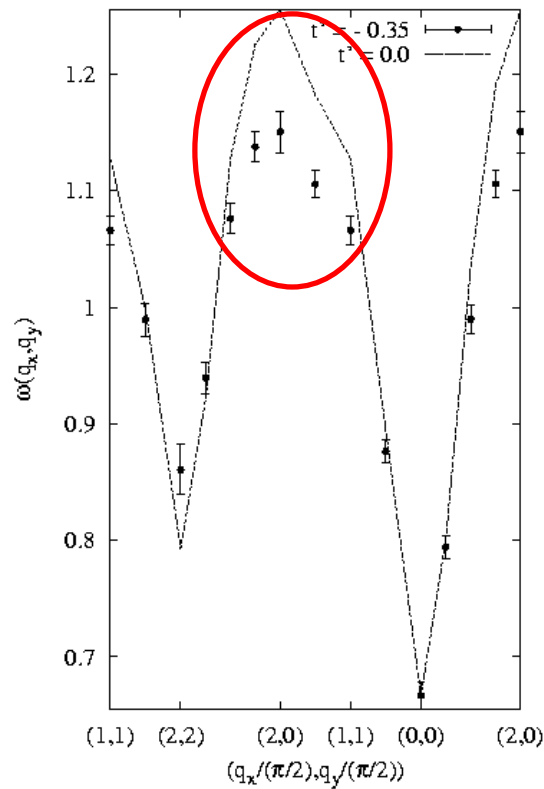
$U = 6$



$U = 0$

What are the results ?

What are the results ?



Spin-wave dispersion,
 $U = 6$, $t' = 0$ and $t' = -0.35$

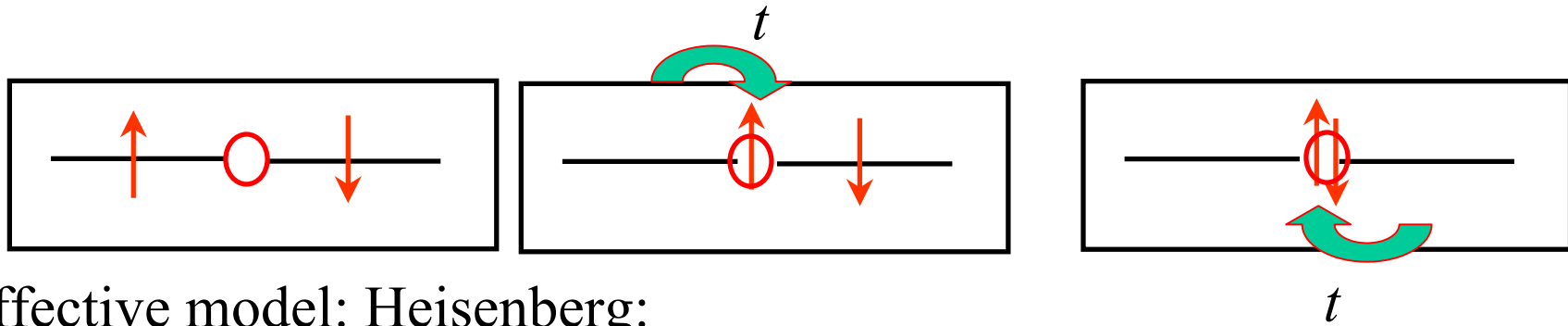
Various values of U

Results

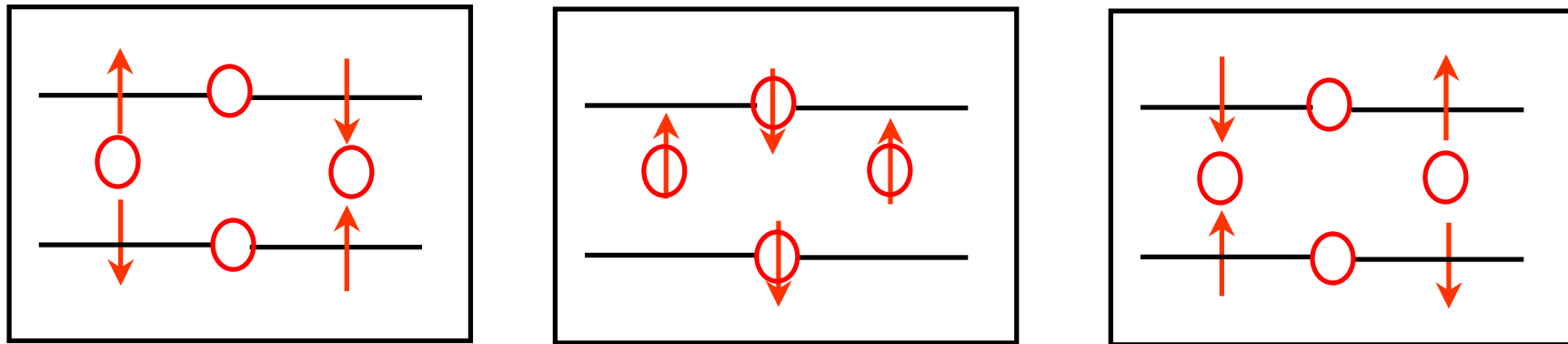
- $U = 5.0 t \pm 0.5 t$ (*cf* $U = 6 t$ when $t' = 0$)
- In agreement with RPA
 - Singh Goswami, Phys. Rev. B **66**, 92402 (2002).
 - Peres, Araujo, Phys. Stat. Sol. **236**, 523 (2003).
- Correction in the wrong direction but this is expected at strong coupling:
 - t' induces antiferromagnetic second-neighbor interaction.
 - Should be ferro. according to linear spin waves

Perspectives

- Single-mode approximation invalid ?
- Should go back to three-band model where link between J and J_c is different.
 - E. Müller-Hartmann and A. Reischl, Eur. Phys. J. B 28, 173 (2002).
- Same Hamiltonian (Hubbard one-band) cannot describe both spin and charge (optical gap) excitations.



Effective model: Heisenberg:

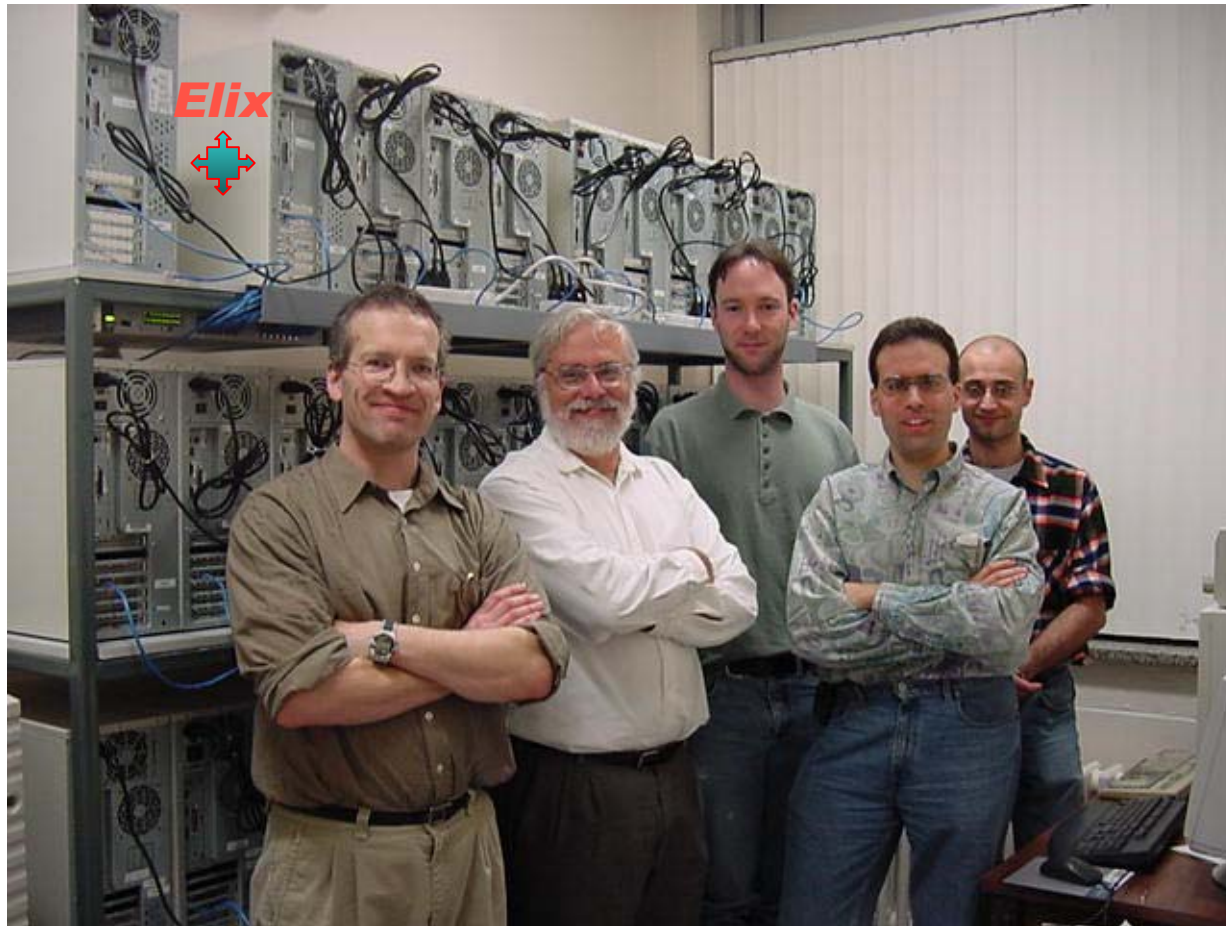


Ring
exchange

and second-neighbor hopping

Michel Barrette

Mehdi Bozzo-Rey



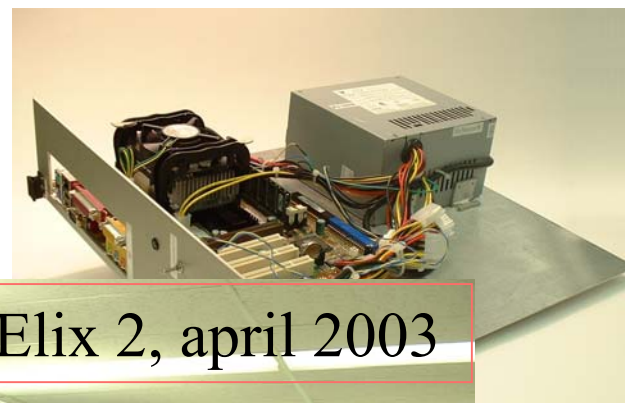
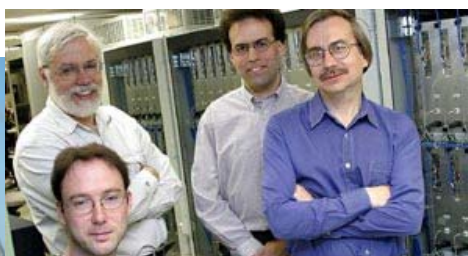
David Sénéchal

A.-M.T.

Alain Veilleux



Carol Gauthier, analyste en Calcul du CCS en plein machinage d'un noeud d'Elix2



Un noeud d'Elix2

Elix 2, avril 2003



Elix2 vu de profil



De gauche à droite: Alain Veilleux, Michel Barrette, Jean-Phillipe Turcotte, Carol Gauthier, Patrick Vachon et le 1er noeud d'Elix



Equipe du CCS devant Elix2. Al'arrière: Patrick Vachon, Minh-Nghia Nguyen, David Lauzon, Michel Barrette, Mehdi Bozzo-Rey, Simon Lessard, Alain Veilleux. A l'avant: Patrice Albaret, Karl Gaven-Venet, Benoît des Ligneris, Francis Giraldeau. Etait absent de la photo: Jean-Philippe Turcotte, Carol Gauthier, Xavier Barnabé Thériault et Mathieu Lutfy





Alexis Gagné-Lebrun

A-M.T. Alexandre Blais Vasyl Hankevych



K. LeHur

C. Bourbonnais



R. Côté



D. Sénéchal



Sébastien Roy

Sarma Kancharla

Bumsoo Kyung

Maxim Mar'enko

C'est fini...

enfin